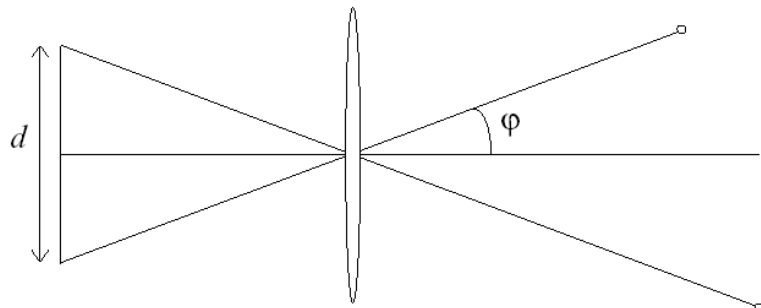
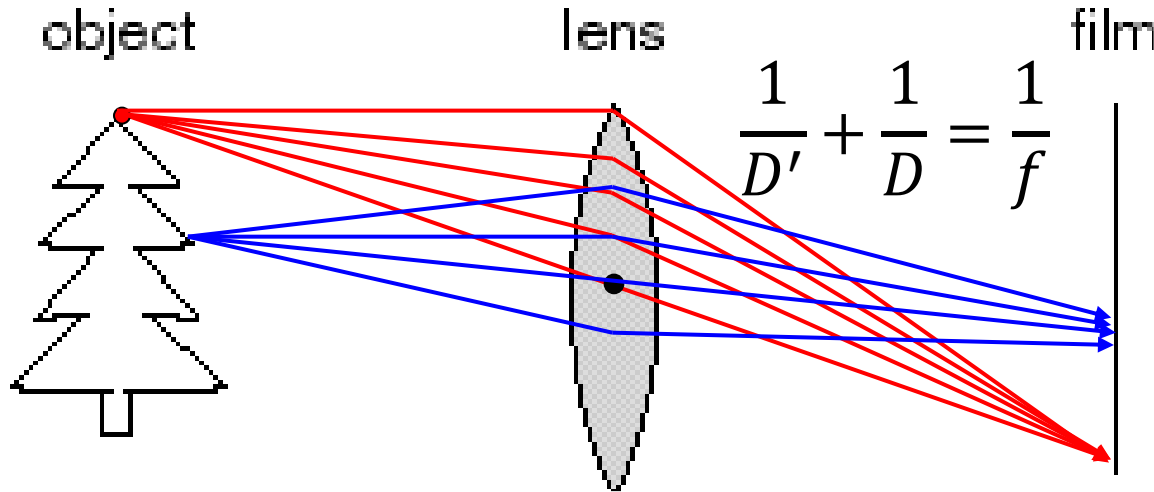
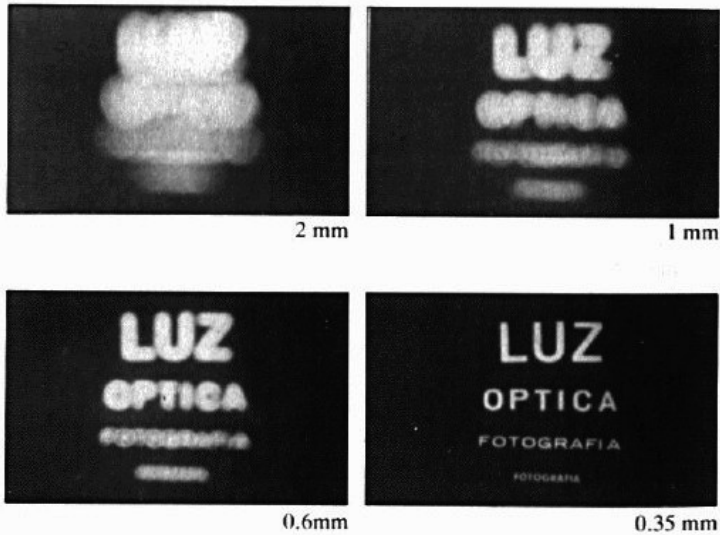

Light, Camera and Shading

CS 543 / ECE 549 – Saurabh Gupta
Spring 2020, UIUC

<http://saurabhg.web.illinois.edu/teaching/ece549/sp2020/>

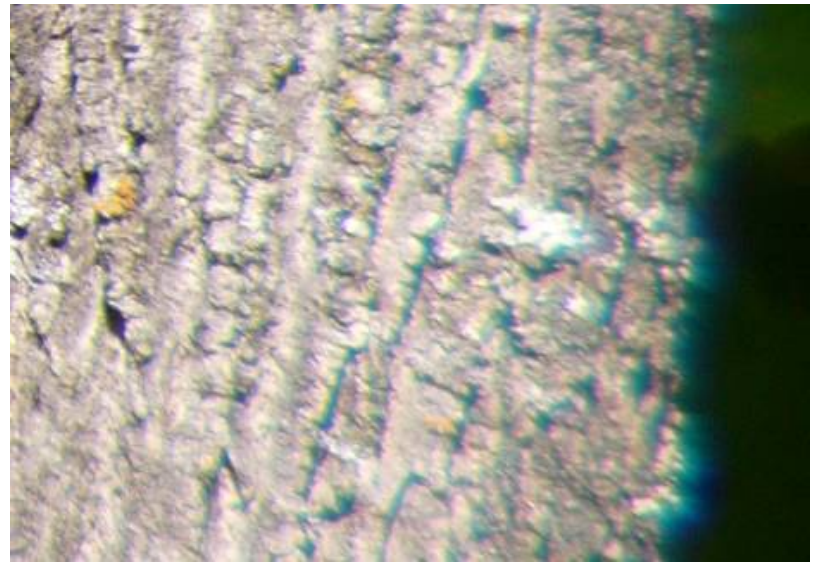
Recap



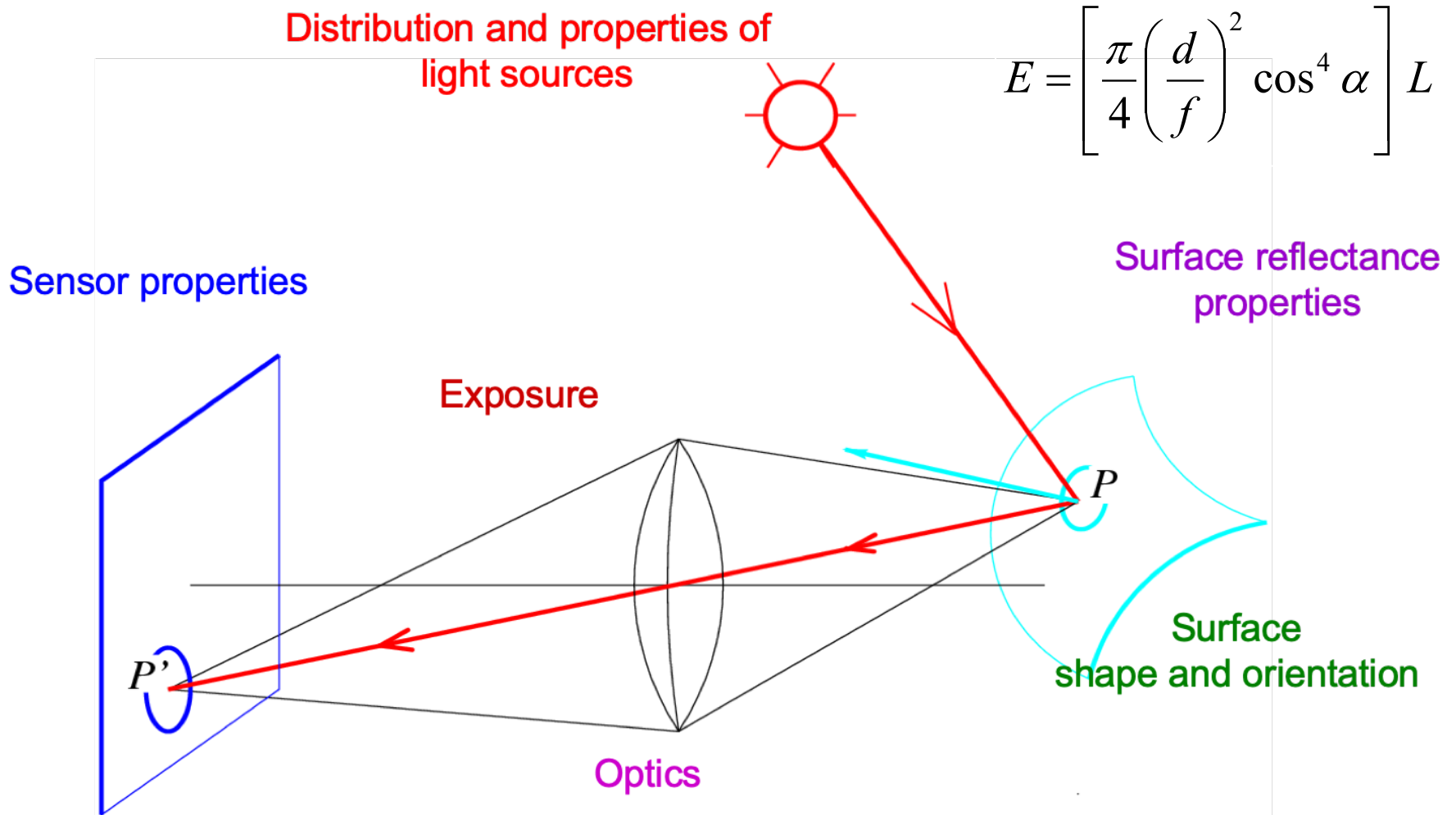
$$\varphi = \tan^{-1} \left(\frac{d}{2f} \right)$$



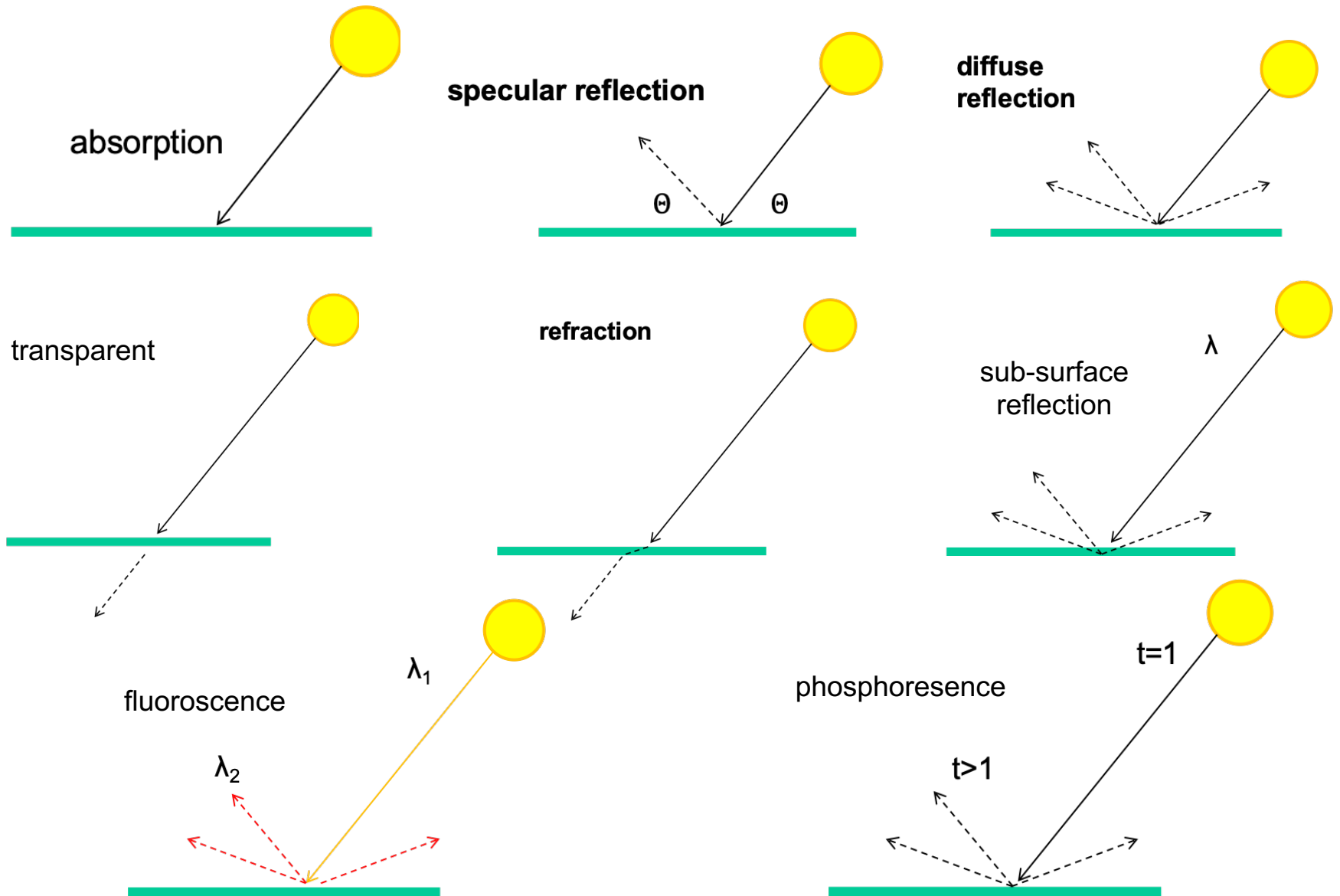
Recap



Recap



Recap



Overview

- Cameras with lenses
 - Depth of field
 - Field of view
 - Lens aberrations
- Brightness of a pixel
 - Small taste of radiometry
 - In-camera transformation of light
 - Reflectance properties of surfaces
 - Lambertian reflection model
 - Shape from shading
- Color

Most surfaces have both

Specularity = spot where specular reflection dominates (typically reflects light source)

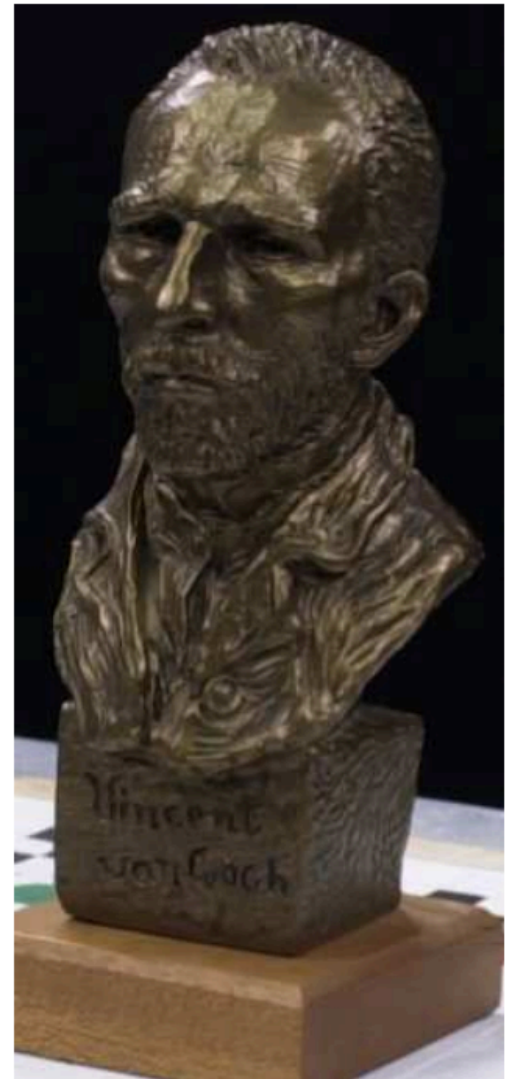


Photo: northcountryhardwoodfloors.com



Typically, specular component is small

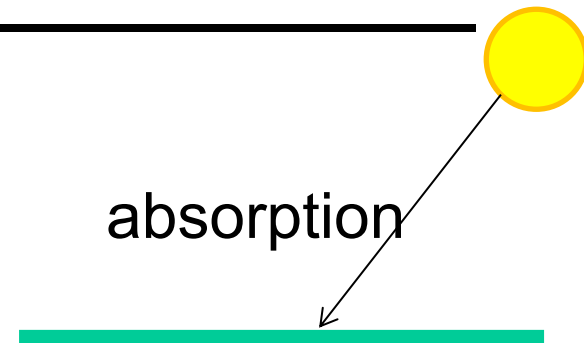
Specular reflection



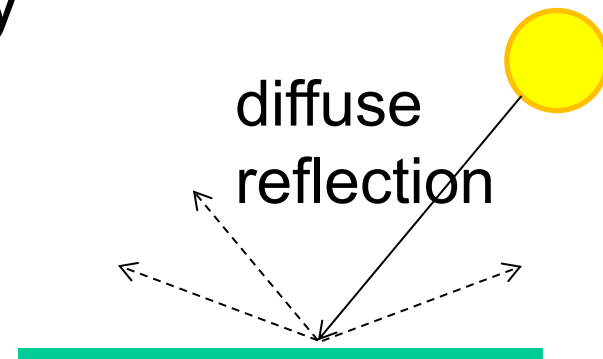
[Picture source](#)

When light hits a typical surface

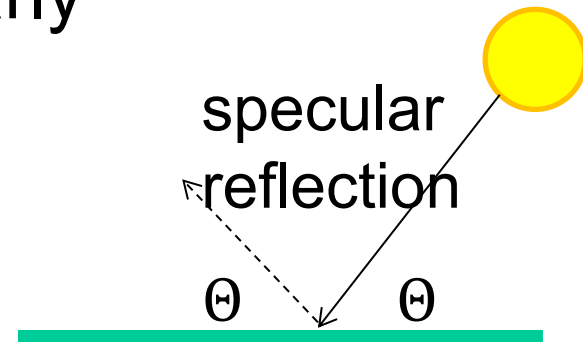
- Some light is absorbed



- Some light is reflected diffusely
 - Independent of viewing direction

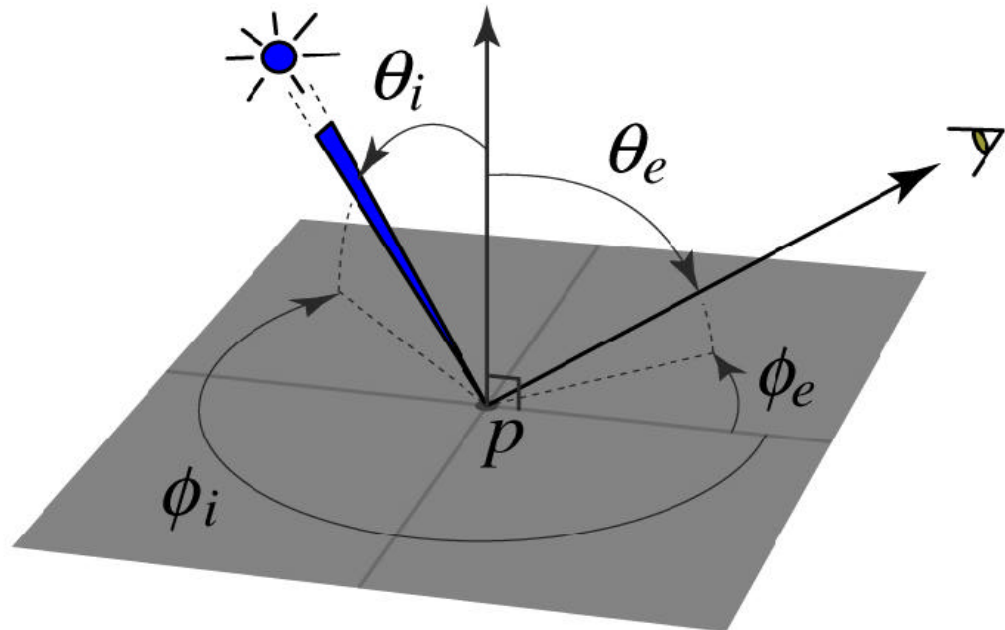


- Some light is reflected specularly
 - Light bounces off (like a mirror), depends on viewing direction



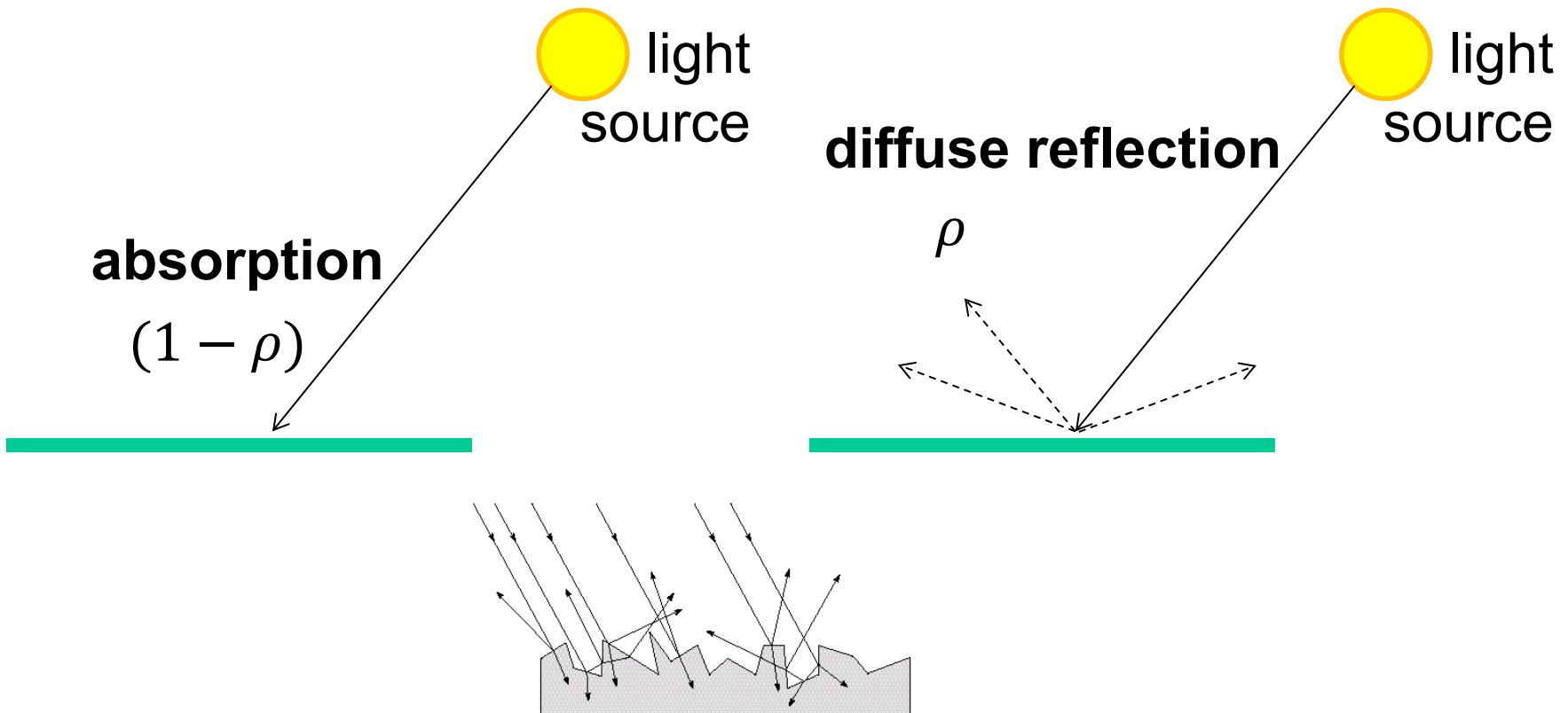
Bidirectional Reflectance Distribution Function (BRDF)

- How bright a surface appears when viewed from one direction when light falls on it from another
- Definition: ratio of the radiance in the emitted direction to irradiance in the incident direction



Lambertian reflectance model

Some light is absorbed (function of albedo ρ)
Remaining light is scattered, *equally* in all directions.
Examples: soft cloth, concrete, matte paints



Intensity and Surface Orientation

Intensity depends on illumination angle because less light comes in at oblique angles.

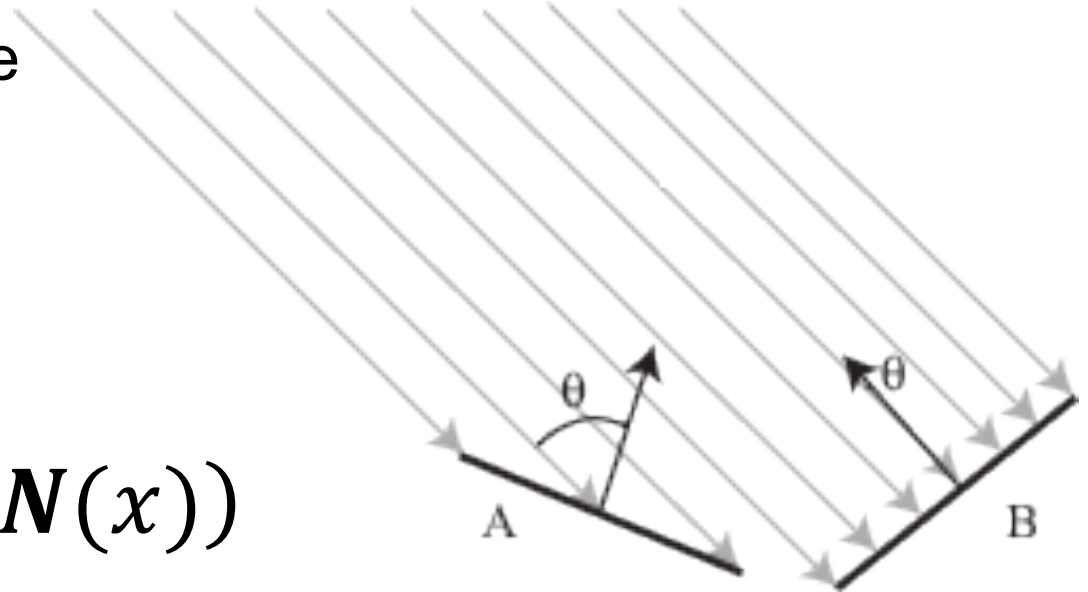
ρ = albedo

\mathbf{S} = directional source

\mathbf{N} = surface normal

I = reflected intensity

$$I(x) = \rho(x)(\mathbf{S} \cdot \mathbf{N}(x))$$



Photometric stereo (shape from shading)

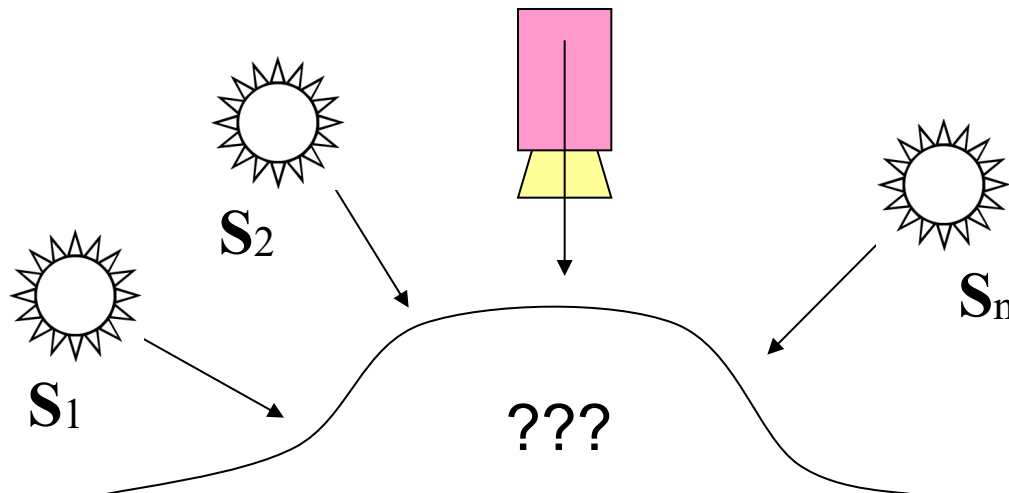
- Can we reconstruct the shape of an object based on shading cues?

Photometric stereo

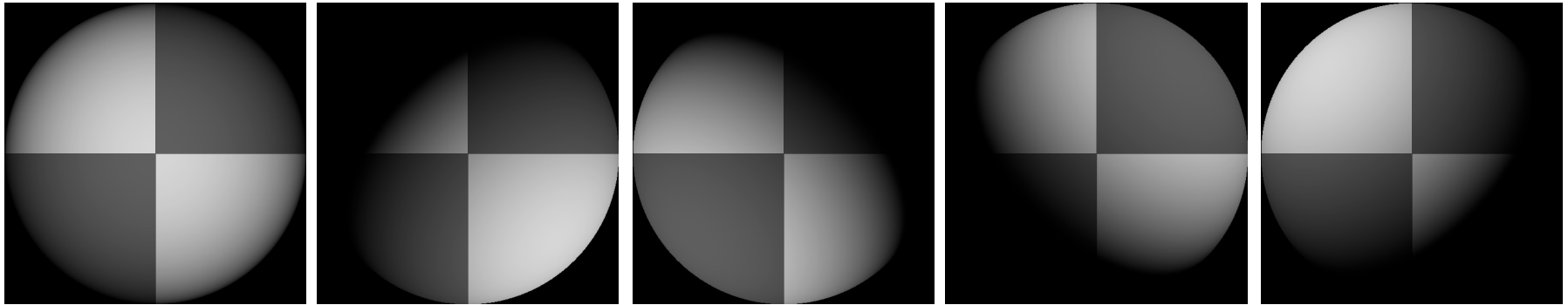
Assume:

- A Lambertian object
- A *local shading model* (each point on a surface receives light only from sources visible at that point)
- A set of *known* light source directions
- A set of pictures of an object, obtained in exactly the same camera/object configuration but using different sources
- Orthographic projection

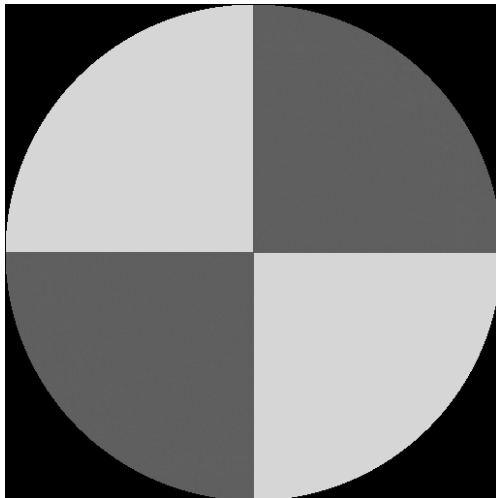
Goal: reconstruct object shape and albedo



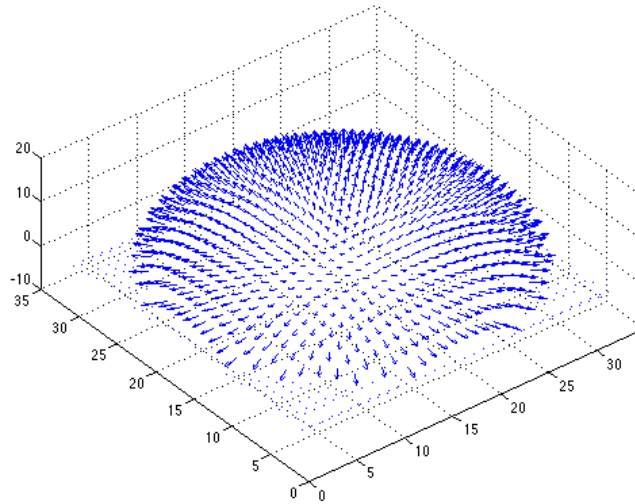
Example 1



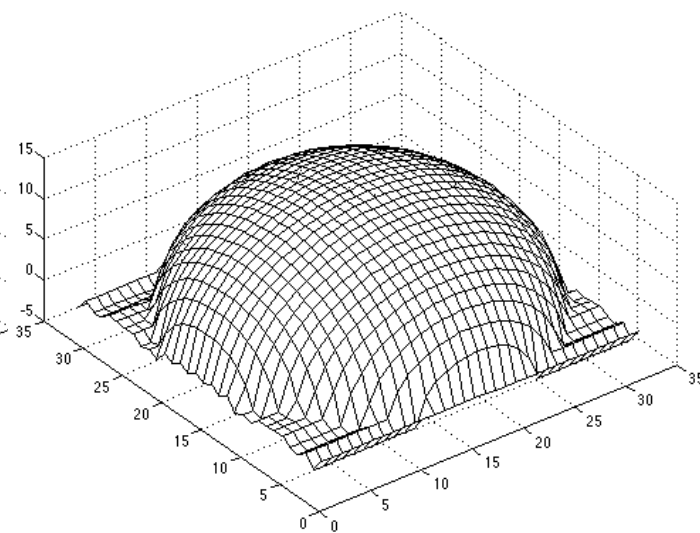
Recovered
albedo



Recovered normal
field



Recovered surface
model



Example 2

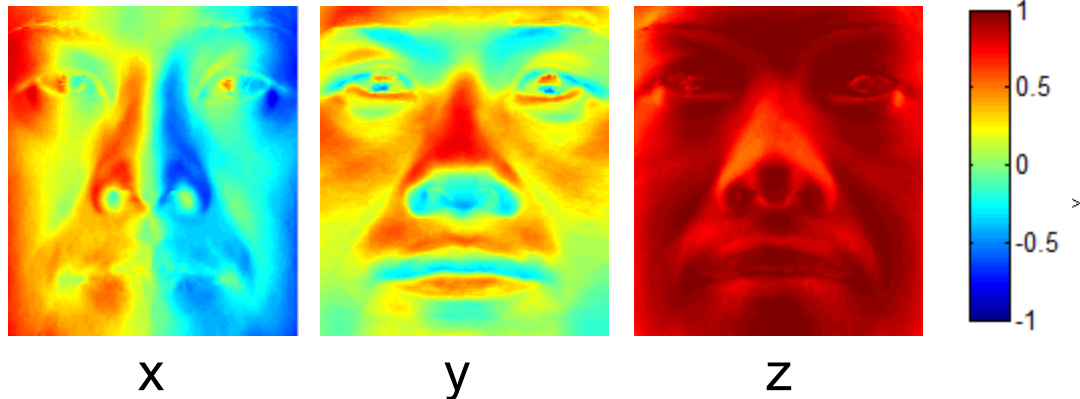
Input



Recovered albedo



Recovered normal field



Recovered surface model



Image model

- **Known:** source vectors S_j and pixel values $I_j(x,y)$
- **Unknown:** surface normal $\mathbf{N}(x,y)$ and albedo $\rho(x,y)$

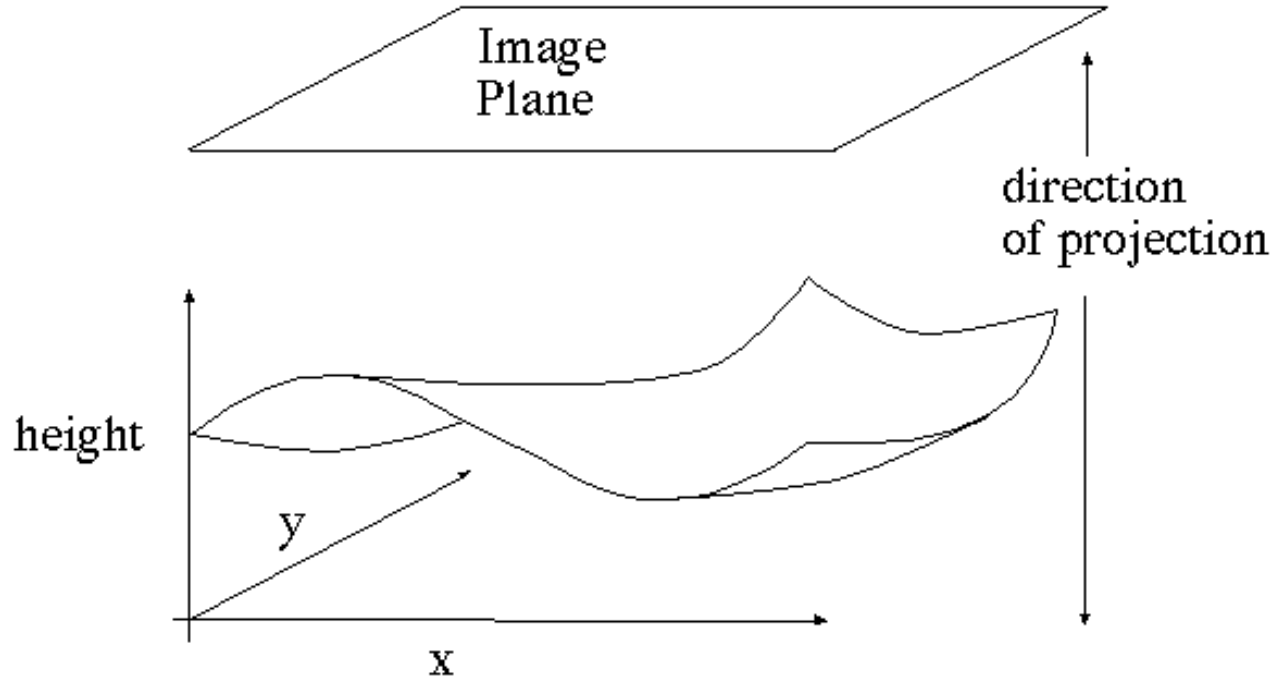


Image model

- **Known:** source vectors \mathbf{S}_j and pixel values $I_j(x,y)$
- **Unknown:** surface normal $\mathbf{N}(x,y)$ and albedo $\rho(x,y)$
- Assume that the response function of the camera is a linear scaling by a factor of k
- Lambert's law:

$$\begin{aligned} I_j(x, y) &= k \rho(x, y) (\mathbf{N}(x, y) \cdot \mathbf{S}_j) \\ &= (\rho(x, y) \mathbf{N}(x, y)) \cdot (k \mathbf{S}_j) \\ &= \mathbf{g}(x, y) \cdot \mathbf{V}_j \end{aligned}$$

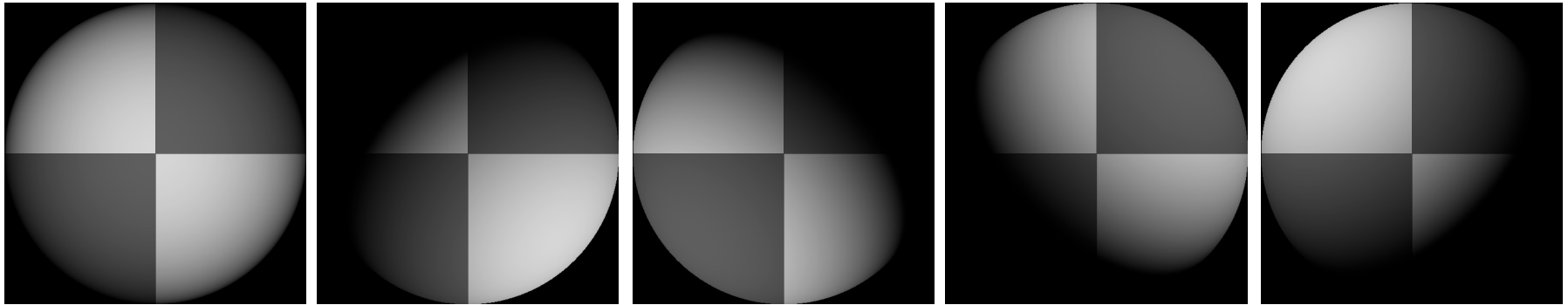
Least squares problem

- For each pixel, set up a linear system:

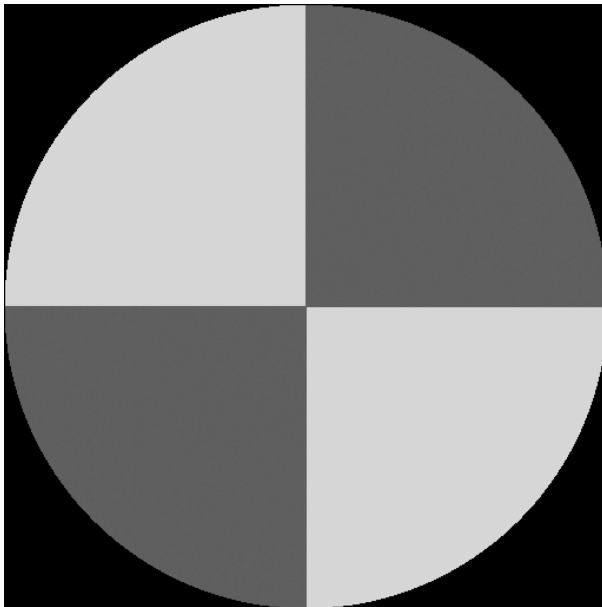
$$\begin{array}{c} \left[\begin{array}{c} I_1(x, y) \\ I_2(x, y) \\ \vdots \\ I_n(x, y) \end{array} \right] = \left[\begin{array}{c} \mathbf{V}_1^T \\ \mathbf{V}_2^T \\ \vdots \\ \mathbf{V}_n^T \end{array} \right] \mathbf{g}(x, y) \\ \begin{array}{ccc} | & | & | \\ (n \times 1) & (n \times 3) & (3 \times 1) \\ \text{known} & \text{known} & \text{unknown} \end{array} \end{array}$$

- Obtain least-squares solution for $\mathbf{g}(x, y)$
(which we defined as $\mathbf{N}(x, y) \rho(x, y)$)
- Since $\mathbf{N}(x, y)$ is the unit normal, $\rho(x, y)$ is given by the magnitude of $\mathbf{g}(x, y)$
- Finally, $\mathbf{N}(x, y) = \mathbf{g}(x, y) / \rho(x, y)$

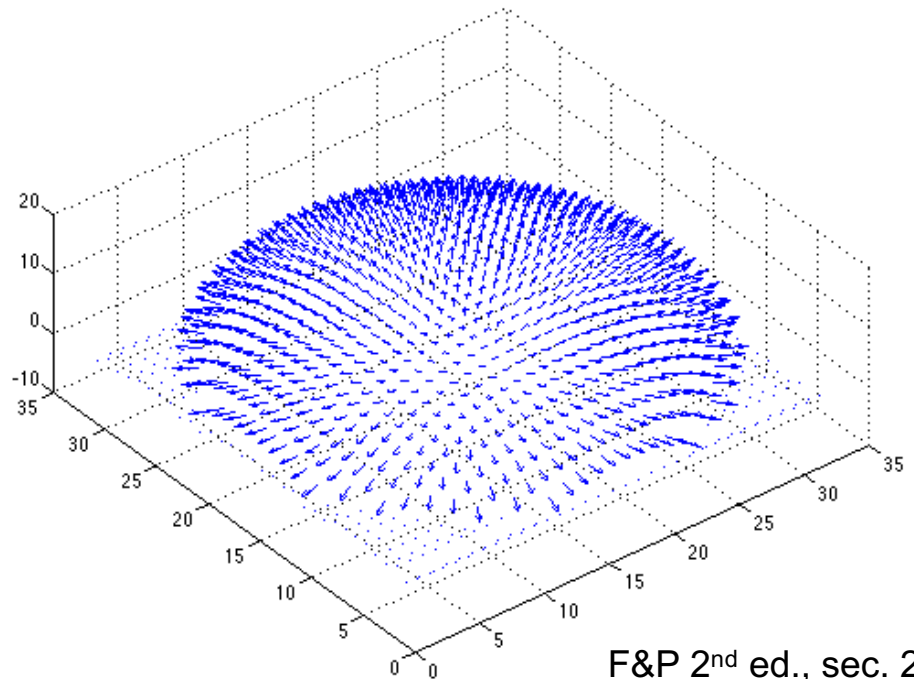
Synthetic example



Recovered albedo



Recovered normal field



Recovering a surface from normals

Recall the surface is written as

$$(x, y, f(x, y))$$

This means the normal has the form:

$$\mathbf{N}(x, y) = \frac{1}{\sqrt{f_x^2 + f_y^2 + 1}} \begin{pmatrix} f_x \\ f_y \\ 1 \end{pmatrix}$$

If we write the estimated vector g as

$$\mathbf{g}(x, y) = \begin{pmatrix} g_1(x, y) \\ g_2(x, y) \\ g_3(x, y) \end{pmatrix}$$

Then we obtain values for the partial derivatives of the surface:

$$f_x(x, y) = g_1(x, y) / g_3(x, y)$$

$$f_y(x, y) = g_2(x, y) / g_3(x, y)$$

Recovering a surface from normals

We can now recover the surface height at any point by integration along some path, e.g.

$$f(x, y) = \int_0^x f_x(s, 0) ds + \int_0^y f_y(x, t) dt + C$$

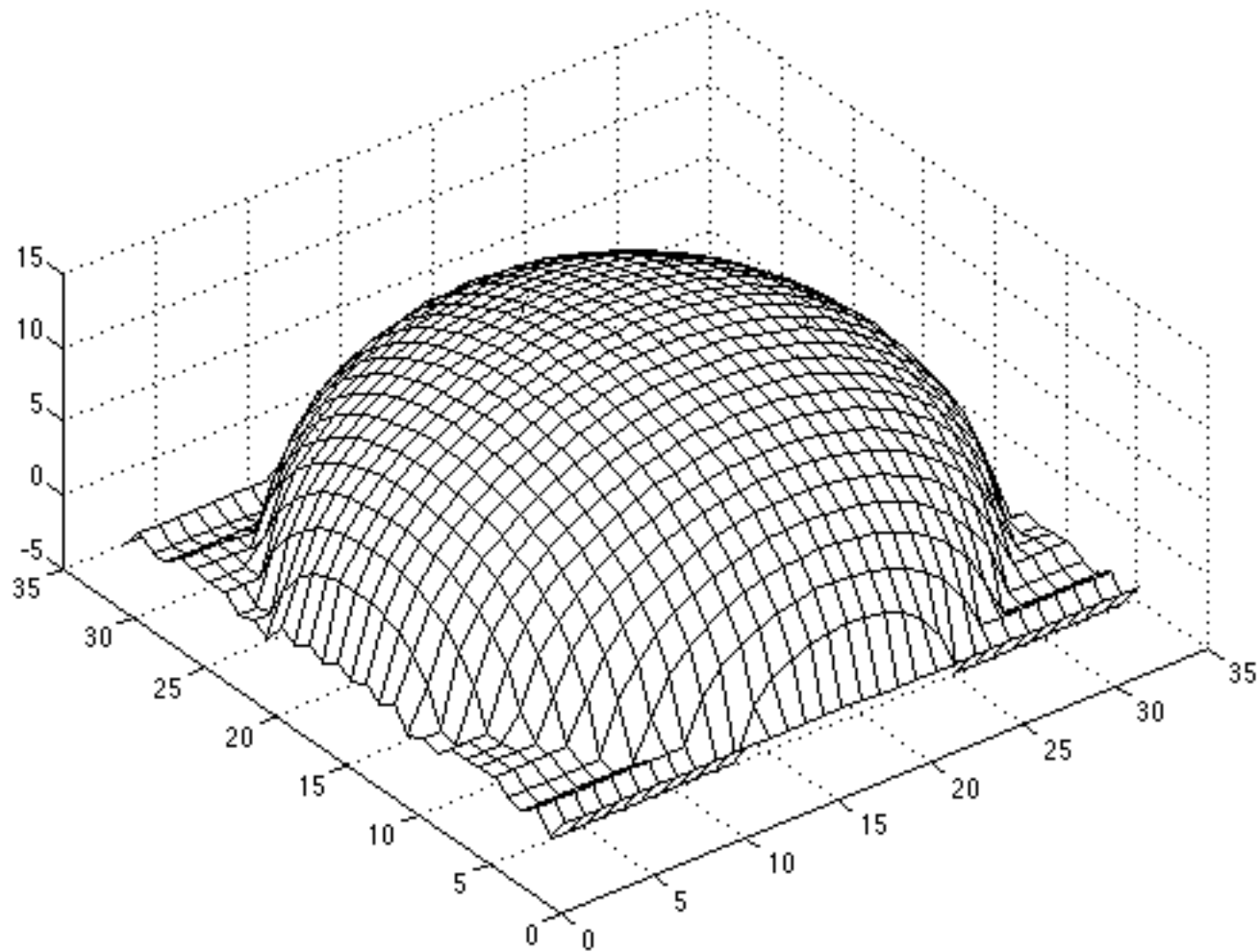
(for robustness, should take integrals over many different paths and average the results)

Integrability: for the surface f to exist, the mixed second partial derivatives must be equal:

$$\frac{\partial}{\partial y} (g_1(x, y) / g_3(x, y)) = \frac{\partial}{\partial x} (g_2(x, y) / g_3(x, y))$$

(in practice, they should at least be similar)

Surface recovered by integration



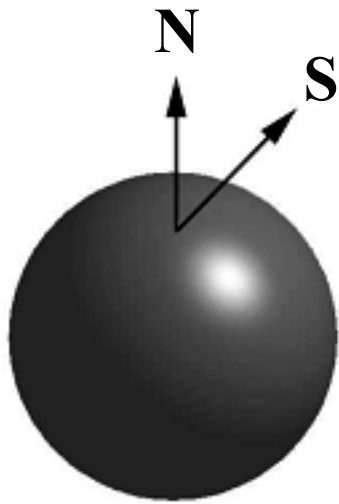
Limitations

- Orthographic camera model
- Simplistic reflectance and lighting model
- No shadows
- No interreflections
- No missing data
- Integration is tricky

Finding the direction of the light source

$$I(x,y) = \mathbf{N}(x,y) \cdot \mathbf{S}(x,y)$$

Full 3D case:

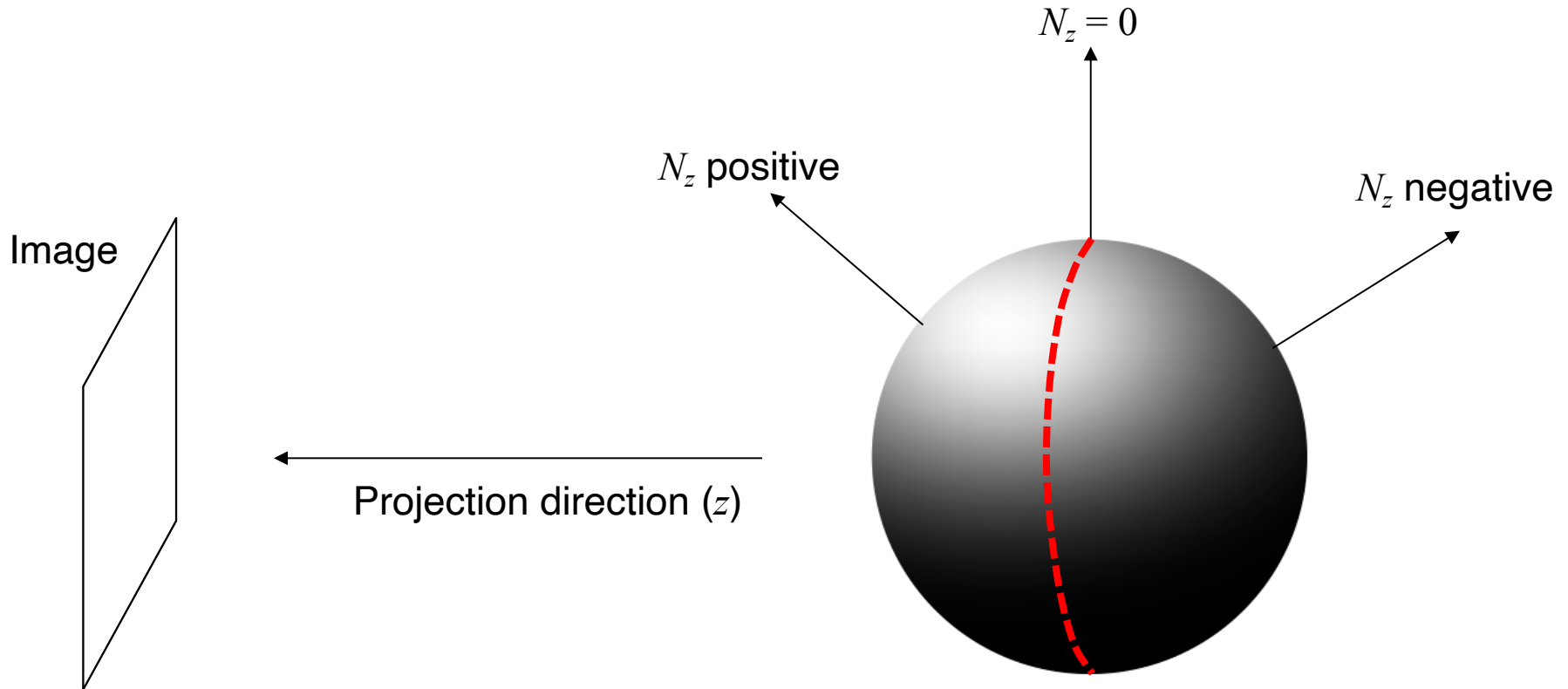


$$\begin{pmatrix} N_x(x_1, y_1) & N_y(x_1, y_1) & N_z(x_1, y_1) \\ N_x(x_2, y_2) & N_y(x_2, y_2) & N_z(x_2, y_2) \\ \vdots & \vdots & \vdots \\ N_x(x_n, y_n) & N_y(x_n, y_n) & N_z(x_n, y_n) \end{pmatrix} \begin{pmatrix} S_x \\ S_y \\ S_z \end{pmatrix} = \begin{pmatrix} I(x_1, y_1) \\ I(x_2, y_2) \\ \vdots \\ I(x_n, y_n) \end{pmatrix}$$

P. Nillius and J.-O. Eklundh, "Automatic estimation of the projected light source direction," CVPR 2001

Finding the direction of the light source

Consider points on the *occluding contour*:



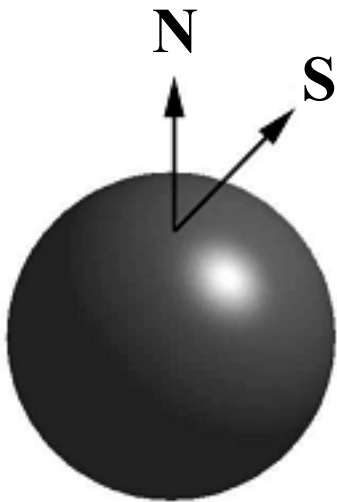
P. Nillius and J.-O. Eklundh, "Automatic estimation of the projected light source direction," CVPR 2001

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For points on the *occluding contour*, $N_z = 0$:

$$\begin{pmatrix} N_x(x_1, y_1) & N_y(x_1, y_1) \\ N_x(x_2, y_2) & N_y(x_2, y_2) \\ \vdots & \vdots \\ N_x(x_n, y_n) & N_y(x_n, y_n) \end{pmatrix} \begin{pmatrix} S_x \\ S_y \end{pmatrix} = \begin{pmatrix} I(x_1, y_1) \\ I(x_2, y_2) \\ \vdots \\ I(x_n, y_n) \end{pmatrix}$$

P. Nillius and J.-O. Eklundh, "Automatic estimation of the projected light source direction," CVPR 2001

Finding the direction of the light source



P. Nillius and J.-O. Eklundh, "Automatic estimation of the projected light source direction," CVPR 2001

Application: Detecting composite photos

Fake photo



Real photo



M. K. Johnson and H. Farid, [Exposing Digital Forgeries by Detecting Inconsistencies in Lighting](#), ACM Multimedia and Security Workshop, 2005.

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