# Neural network training: The basics and beyond

Slides from Lana Lazebnik

### Outline

- Optimization
  - Mini-batch SGD
  - Learning rate decay
  - Diagnosing learning curves
  - Adaptive optimization methods: SGD with momentum, RMSProp, Adam
- Massaging the numbers
  - Data augmentation
  - Data preprocessing
  - Weight initialization
  - Batch normalization
- Regularization
- Test time: averaging predictions, ensembles

### Mini-batch SGD

- Iterate over epochs
  - Group data into mini-batches of size *b* 
    - Compute gradient of the loss for the mini-batch  $(x_1, y_1), \dots, (x_b, y_b)$ :

$$\nabla \hat{L} = \frac{1}{b} \sum_{i=1}^{b} \nabla l(w, x_i, y_i)$$

• Update parameters:

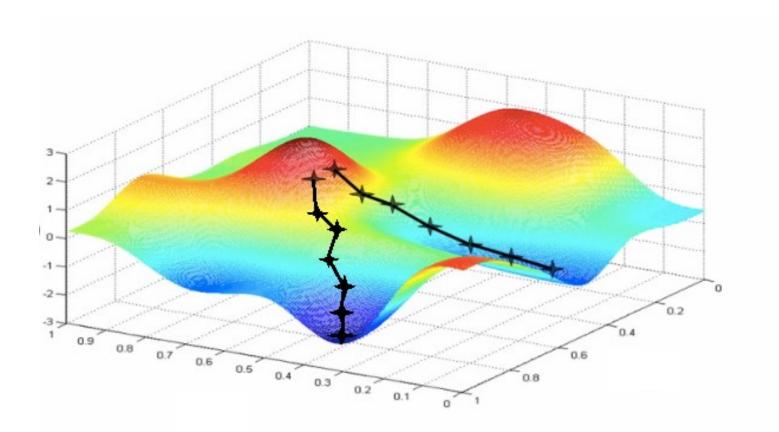
$$w \leftarrow w - \eta \nabla \widehat{L}$$

- Check for convergence, decide whether to decay learning rate
- What are the hyperparameters?
  - Mini-batch size, learning rate decay schedule, deciding when to stop

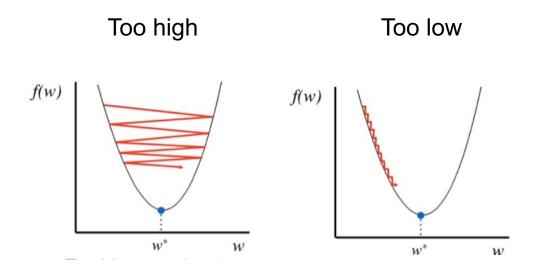
### Setting the mini-batch size

- Smaller mini-batches: less memory overhead, less parallelizable, more gradient noise (which could work as regularization – see, e.g., <u>Keskar et al.</u>, 2017)
- Larger mini-batches: more expensive and less frequent updates, lower gradient variance, more parallelizable.
  Can be made to work well with good choices of learning rate and other aspects of optimization (<u>Goyal et al.</u>, 2018)

### Setting the learning rate



### Setting the learning rate



Want: good decay schedule

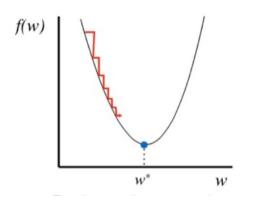
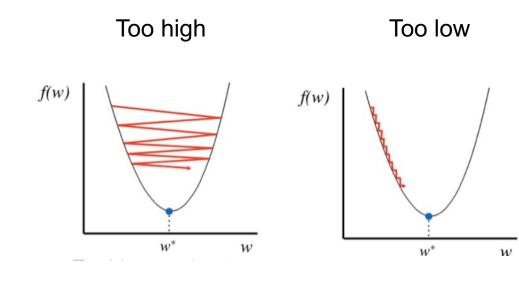
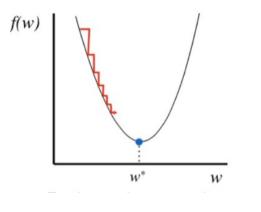


Figure source

### Setting the learning rate



Want: good decay schedule



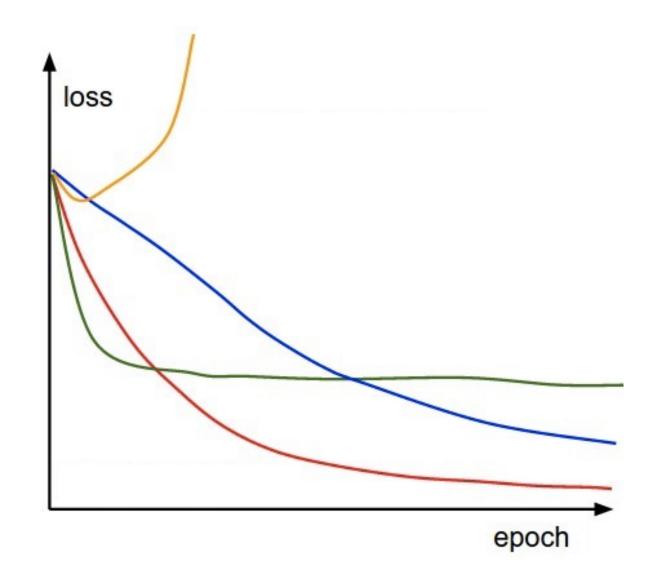


Figure source

Source: Stanford CS231n

### Learning rate decay

- Decay formulas
  - Exponential:  $\eta_t = \eta_0 e^{-kt}$ , where  $\eta_0$  and k are hyperparameters, t is the iteration or epoch number
  - Inverse:  $\eta_t = \eta_0/(1+kt)$
  - Inverse sqrt:  $\eta_t = \eta_0 / \sqrt{t}$
  - Linear:  $\eta_t = \eta_0(1 t/T)$ , where *T* is the total number of epochs
  - Cosine:  $\eta_t = \frac{1}{2}\eta_0(1 + \cos(t\pi/T))$

### Learning rate decay

- Decay formulas
- Most common in practice:
  - Step decay: reduce rate by a constant factor every few epochs, e.g., by 0.5 every 5 epochs, 0.1 every 20 epochs
  - Manual: watch validation error and reduce learning rate whenever it stops improving
    - "Patience" hyperparameter: number of epochs without improvement before reducing learning rate

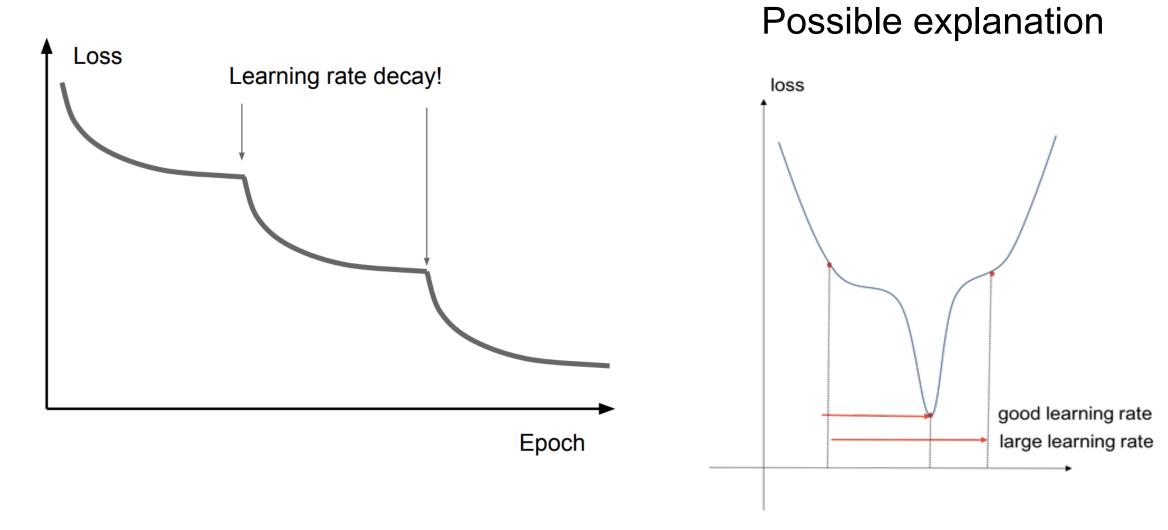
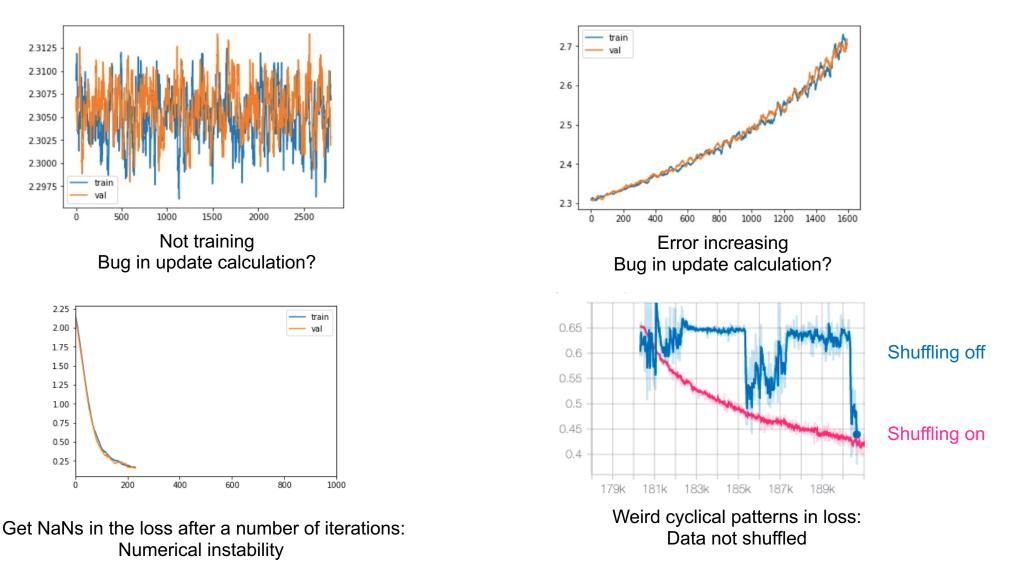


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### Learning rate decay

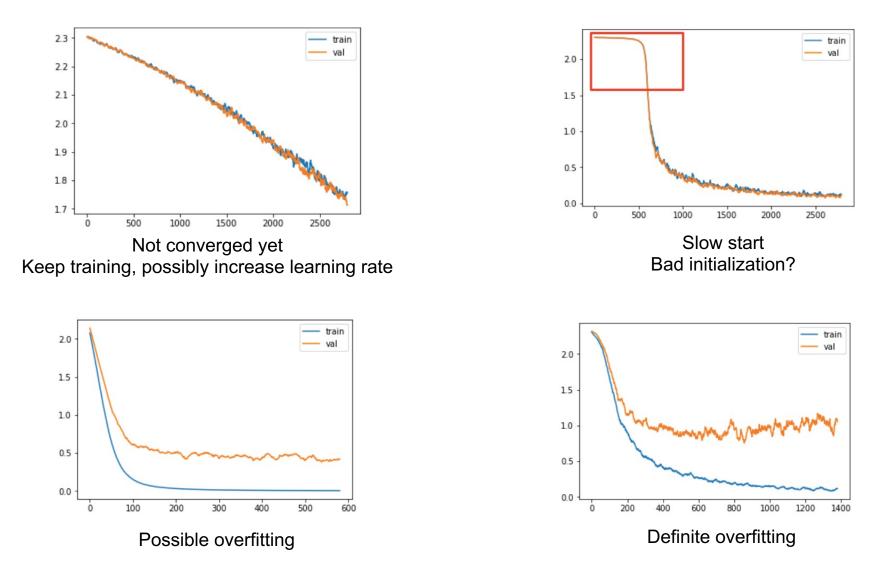
- Decay formulas
- Most common in practice:
  - **Step decay:** reduce rate by a constant factor every few epochs, e.g., by 0.5 every 5 epochs, 0.1 every 20 epochs
  - Manual: watch validation error and reduce learning rate whenever it stops improving
    - "Patience" hyperparameter: number of epochs without improvement before reducing learning rate
- Warmup: train with a low learning rate for a first few epochs, or linearly increase learning rate before transitioning to normal decay schedule (<u>Goyal et al.</u>, 2018)

#### Diagnosing learning curves: Obvious problems



Source: Stanford CS231n

#### Diagnosing learning curves: Subtler behaviors



Source: Stanford CS231n

## When to stop training?

- Monitor validation error to decide when to stop
  - "Patience" hyperparameter: number of epochs without improvement before stopping
  - *Early stopping* can be viewed as a kind of regularization

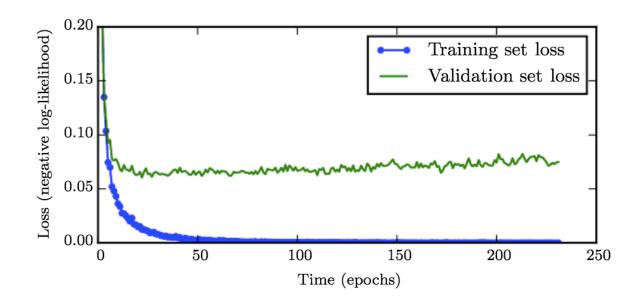
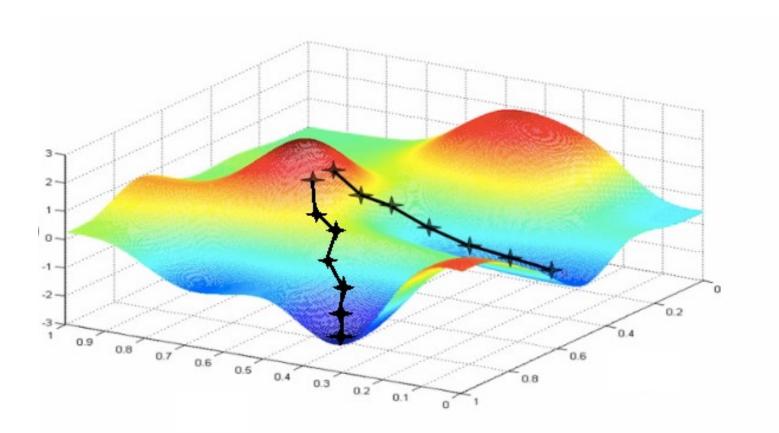


Figure from **Deep Learning Book** 

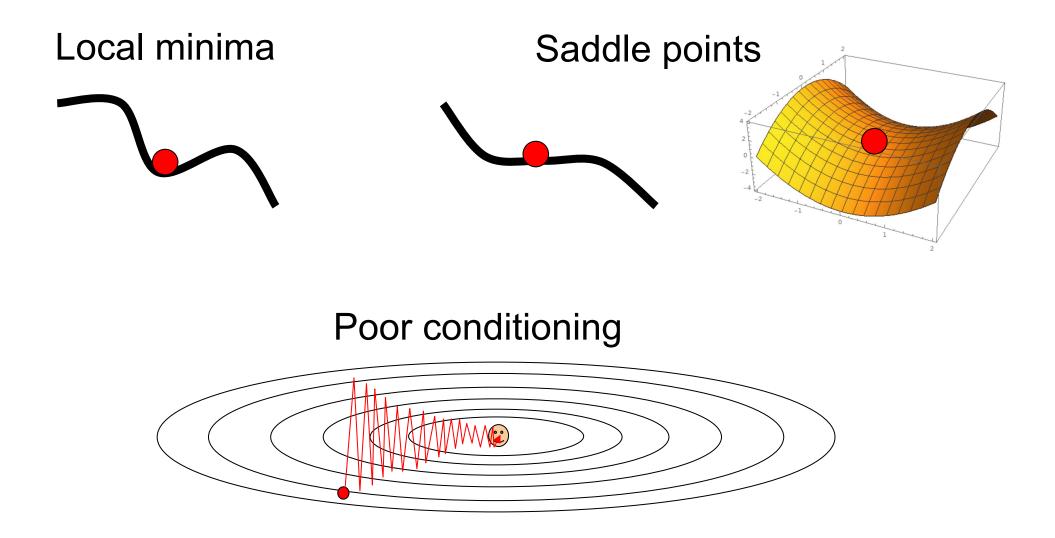
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#### Where does SGD run into trouble?



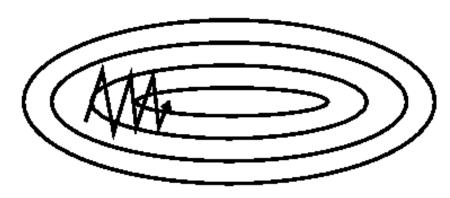
#### Where does SGD run into trouble?



Source: J. Johnson

### SGD with momentum

• Goal: move faster in directions with consistent gradient, avoid oscillating in directions with large but inconsistent gradients



**Standard SGD** 

SGD with momentum

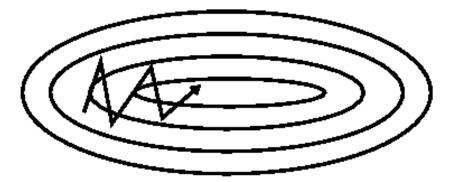




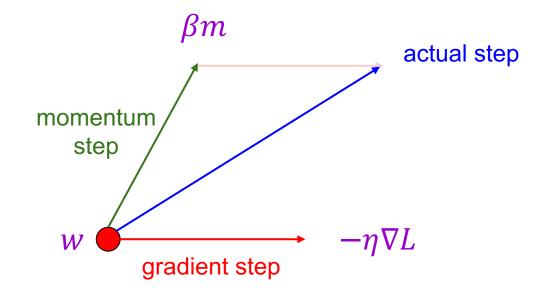
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### SGD with momentum

Introduce a "momentum" variable *m* and associated "friction" coefficient β:

 $m \leftarrow \beta m - \eta \nabla L$  $w \leftarrow w + m$ 

• Typically start with  $\beta = 0.5$ , gradually increase over time





### Adagrad: Adaptive per-parameter learning rates

- Keep track of history of gradient magnitudes, scale the learning rate for each parameter based on this history
- For each dimension *k* of the weight vector:

$$v^{(k)} \leftarrow v^{(k)} + \left(\frac{\partial L}{\partial w^{(k)}}\right)^{2}$$
$$w^{(k)} \leftarrow w^{(k)} - \frac{\eta}{\sqrt{v^{(k)}} + \epsilon} \frac{\partial L}{\partial w^{(k)}}$$

Update running sum of squared magnitudes of gradient w.r.t. *k*th weight

Scale learning rate for *k*th weight by inverse of the magnitude, update *k*th weight

- Parameters with small gradients get large updates and vice versa
- Problem: long-ago gradient magnitudes are not "forgotten" so learning rate decays too quickly

J. Duchi, <u>Adaptive subgradient methods for online learning and stochastic optimization</u>, JMLR 2011

#### RMSProp

• Introduce decay factor  $\beta$  (typically  $\geq 0.9$ ) to downweight past history exponentially:

$$v^{(k)} \leftarrow \beta v^{(k)} + (1 - \beta) \left(\frac{\partial L}{\partial w^{(k)}}\right)^2$$

$$w^{(k)} \leftarrow w^{(k)} - \frac{\eta}{\sqrt{v^{(k)}} + \epsilon} \frac{\partial L}{\partial w^{(k)}}$$

http://www.cs.toronto.edu/~tijmen/csc321/slides/lecture\_slides\_lec6.pdf

#### Adam: Combine RMSProp with momentum

• Update momentum:

 $m \leftarrow \beta_1 m + (1 - \beta_1) \nabla L$ 

• For each dimension *k* of the weight vector:

$$\psi^{(k)} \leftarrow \beta_2 \psi^{(k)} + (1 - \beta_2) \left(\frac{\partial L}{\partial w^{(k)}}\right)^2$$
$$w^{(k)} \leftarrow w^{(k)} - \frac{\eta}{\sqrt{\psi^{(k)}} + \epsilon} m^{(k)}$$

- Full algorithm includes *bias correction* to account for *m* and *v* starting at 0:  $\hat{m} = \frac{m}{1-\beta_1^t}$ ,  $\hat{v} = \frac{v}{1-\beta_2^t}$  (*t* is the timestep)
- Default parameters from paper are reputed to work well for many models:  $\beta_1 = 0.9$ ,  $\beta_2 = 0.999$ ,  $\eta = 1e 3$ ,  $\epsilon = 1e 8$

D. Kingma and J. Ba, Adam: A method for stochastic optimization, ICLR 2015

### Which optimizer to use in practice?

- Adaptive methods tend to reduce initial training error faster than SGD and are "safer"
  - Andrej Karpathy: "In the early stages of setting baselines I like to use Adam with a learning rate of 3e-4. In my experience Adam is much more forgiving to hyperparameters, including a bad learning rate. For ConvNets a well-tuned SGD will almost always slightly outperform Adam, but the optimal learning rate region is much more narrow and problem-specific."
  - Use Adam early in training, switch to SGD for later epochs?

#### Which optimizer to use in practice?

- Adaptive methods tend to reduce initial training error faster than SGD and are "safer"
- Some literature has reported problems with adaptive methods, such as failing to converge or generalizing poorly (<u>Wilson et al.</u> 2017, <u>Reddi et al.</u> 2018)
- More recent comparative study (<u>Schmidt et al.</u>, 2021): "We observe that evaluating multiple optimizers with default parameters works approximately as well as tuning the hyperparameters of a single, fixed optimizer."

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  - Data preprocessing
  - Weight initialization
  - Batch normalization

- Introduce transformations not adequately sampled in the training data
  - Geometric: flipping, rotation, shearing, multiple crops

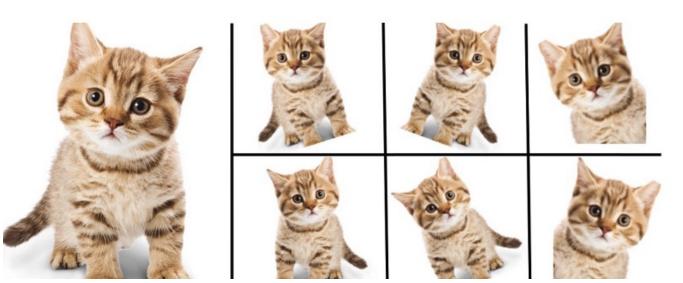


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- Introduce transformations not adequately sampled in the training data
  - Geometric: flipping, rotation, shearing, multiple crops
  - Photometric: color transformations

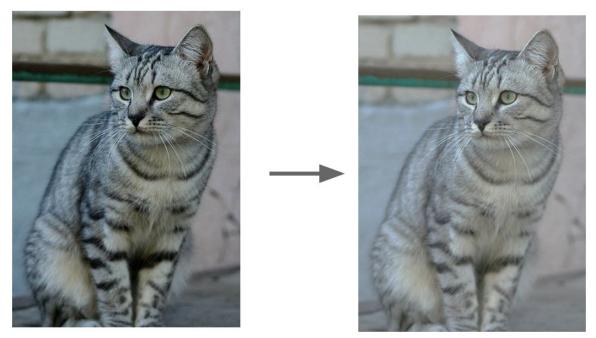
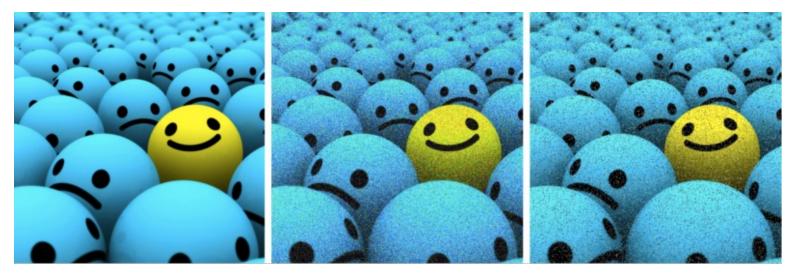


Image source

- Introduce transformations not adequately sampled in the training data
  - Geometric: flipping, rotation, shearing, multiple crops
  - Photometric: color transformations
  - Other: add noise, compression artifacts, lens distortions, etc.

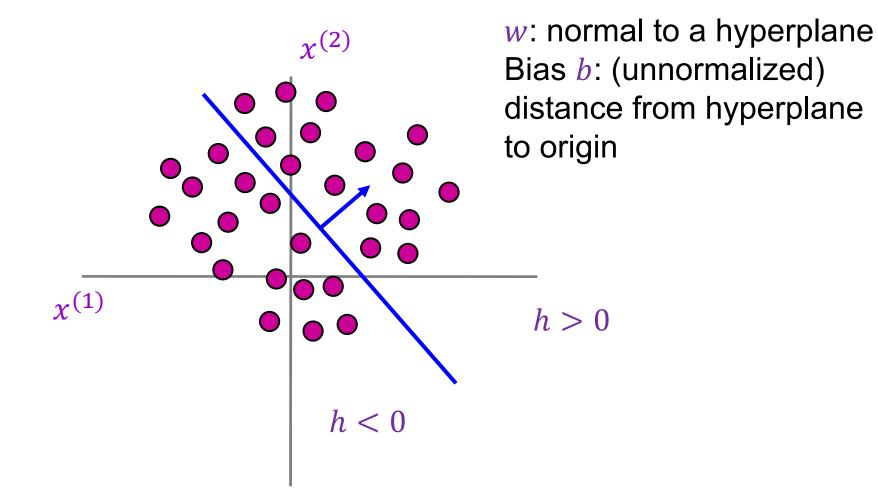


- Introduce transformations not adequately sampled in the training data
- Limited only by your imagination and time/memory constraints!
- Avoid introducing artifacts
- Automatic augmentation strategies: <u>AutoAugment</u>, <u>RandAugment</u>

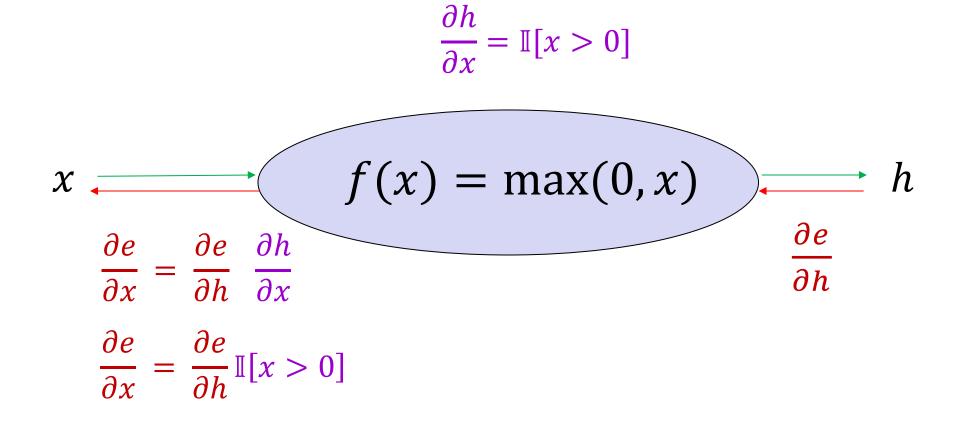
### Data preprocessing

- Zero centering
  - Subtract mean image all input images need to have the same resolution
  - Subtract *per-channel means* images don't need to have the same resolution
- Optional: rescaling divide each value by (per-pixel or perchannel) standard deviation
- Be sure to apply the same transformation at training and test time!
  - Save training set statistics and apply to test data

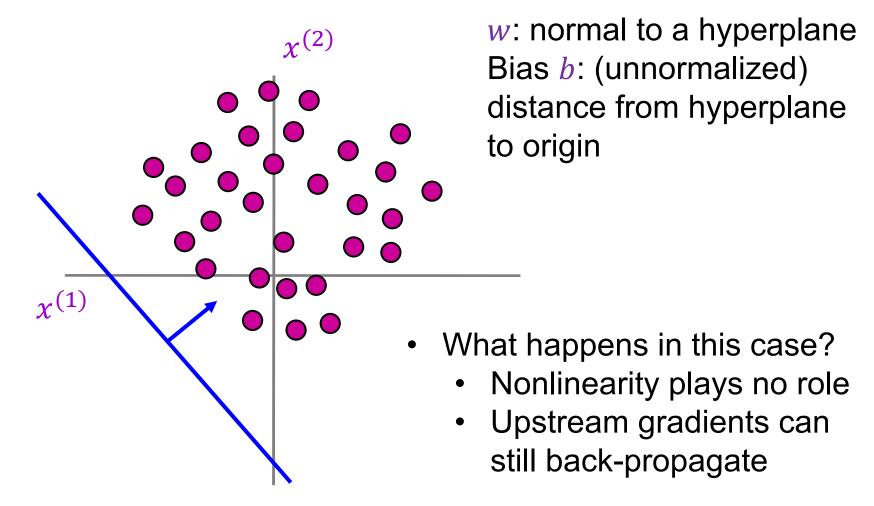
• Consider the behavior of a linear+ReLU unit:  $h = \text{ReLU}(w^T x + b)$ 

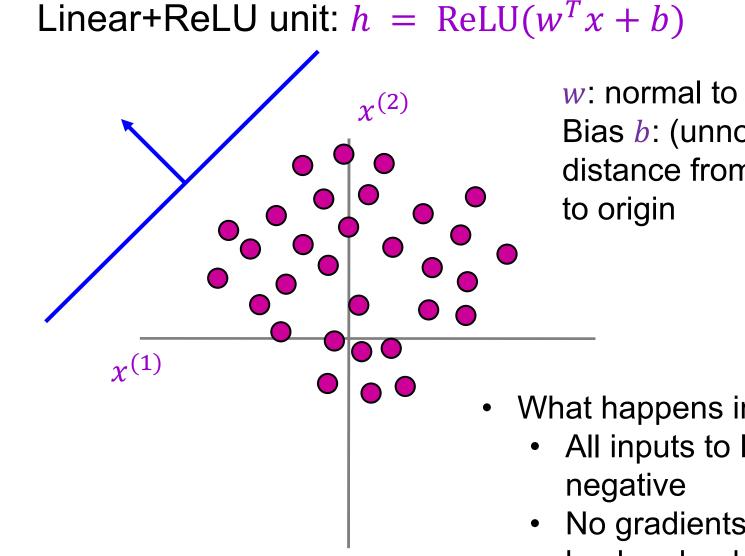


#### **Review: Backward pass for ReLU**



Linear+ReLU unit:  $h = \text{ReLU}(w^T x + b)$ 





w: normal to a hyperplane Bias *b*: (unnormalized) distance from hyperplane

- What happens in this case?
  - All inputs to ReLU are
  - No gradients propagate back - dead ReLU!

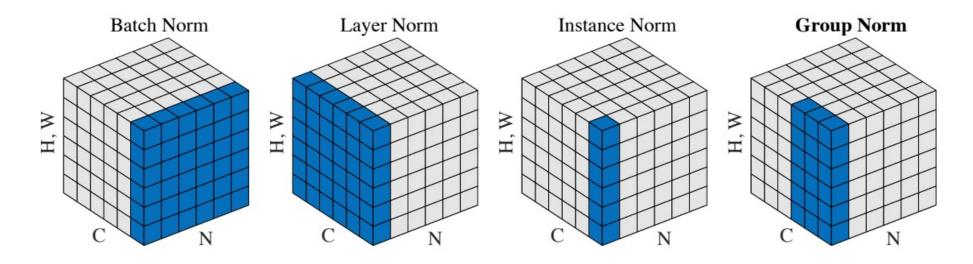
• What's wrong with initializing all weights to the same number (e.g., zero)?

## Weight initialization

- Typically: initialize to random values sampled from zeromean Gaussian:  $w \sim \mathcal{N}(0, \sigma^2)$ 
  - Standard deviation matters!
  - Key idea: avoid reducing or amplifying the variance of layer responses, which would lead to vanishing or exploding gradients
- Common heuristics:
  - Xavier initialization:  $\sigma^2 = 1/n_{in}$  or  $\sigma^2 = 2/(n_{in} + n_{out})$ , where  $n_{in}$  and  $n_{out}$  are the numbers of inputs and outputs to a layer (Glorot and Bengio, 2010)
  - Kaiming initialization (goes with ReLU):  $\sigma^2 = 2/n_{in}$  (<u>He et al.</u>, 2015)
- Initializing biases: just set them to 0

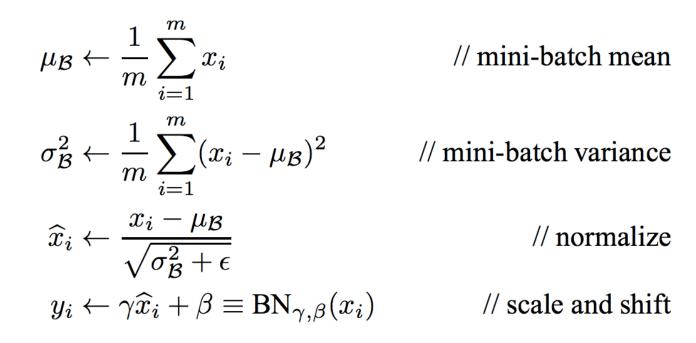
## Normalization

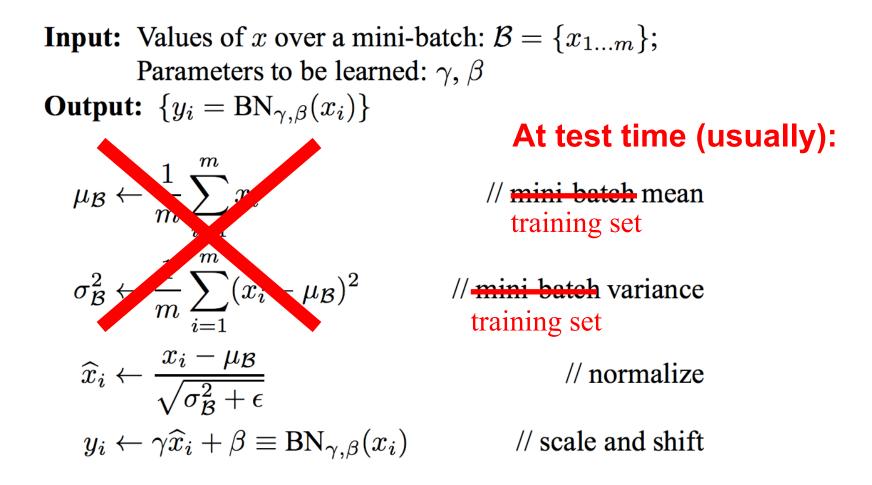
- I omitted a crucial detail so far:
  - It is often useful to standardize statistics of hidden layers
  - through use of *normalization layers*
  - to mitigate vanishing / exploding gradients
  - when training deeper networks
- Many forms of normalization:



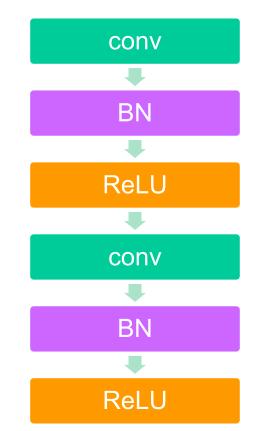
- **Key idea:** shifting and rescaling are differentiable operations, so the network can *learn* how to best normalize the data
- Statistics of activations (outputs) from a given layer across the dataset can be approximated by statistics from a minibatch

Input: Values of x over a mini-batch:  $\mathcal{B} = \{x_{1...m}\};$ Parameters to be learned:  $\gamma, \beta$ Output:  $\{y_i = BN_{\gamma,\beta}(x_i)\}$ 





• Common configuration: insert BN layers right after conv or FC layers, before ReLU nonlinearity (but this is purely empirical)



- Benefits
  - Prevents exploding and vanishing gradients
  - Keeps most activations away from saturation regions of non-linearities
  - Accelerates convergence of training
  - Makes training more robust w.r.t. hyperparameter choice, initialization
- Pitfalls
  - Behavior depends on composition of mini-batches, can lead to hard-tocatch bugs if there is a mismatch between training and test regime (<u>example</u>)
  - Doesn't work well for small mini-batch sizes
  - Cannot be used for certain types of models (recurrent models, transformers)

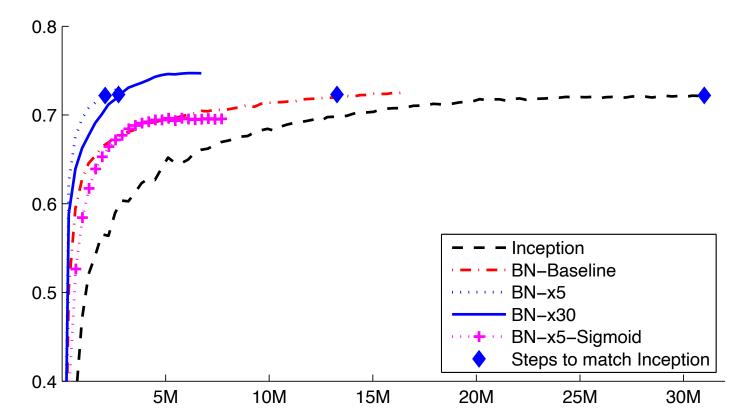
*Inception*: the network described at the beginning of Section 4.2, trained with the initial learning rate of 0.0015.

*BN-Baseline*: Same as Inception with Batch Normalization before each nonlinearity.

BN-x5: Inception with Batch Normalization and the modifications in Sec. 4.2.1. The initial learning rate was increased by a factor of 5, to 0.0075. The same learning rate increase with original Inception caused the model parameters to reach machine infinity.

BN-x30: Like BN-x5, but with the initial learning rate 0.045 (30 times that of Inception).

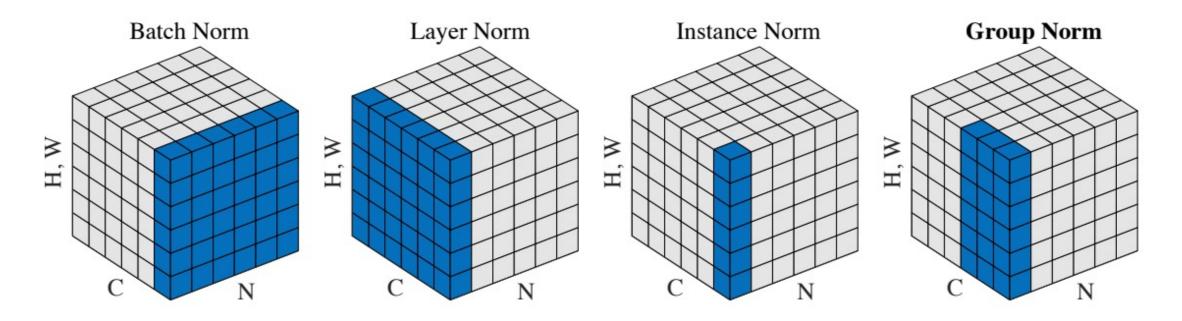
*BN-x5-Sigmoid*: Like *BN-x5*, but with sigmoid nonlinearity  $g(t) = \frac{1}{1+\exp(-x)}$  instead of ReLU. We also attempted to train the original Inception with sigmoid, but the model remained at the accuracy equivalent to chance.



S. lofffe and C. Szegedy, <u>Batch Normalization: Accelerating Deep Network Training by</u> <u>Reducing Internal Covariate Shift</u>, arXiv 2015

## Other types of normalization

- Layer normalization (Ba et al., 2016)
- Instance normalization (Ulyanov et al., 2017)
- Group normalization (Wu and He, 2018)
- Weight normalization (Salimans et al., 2016)



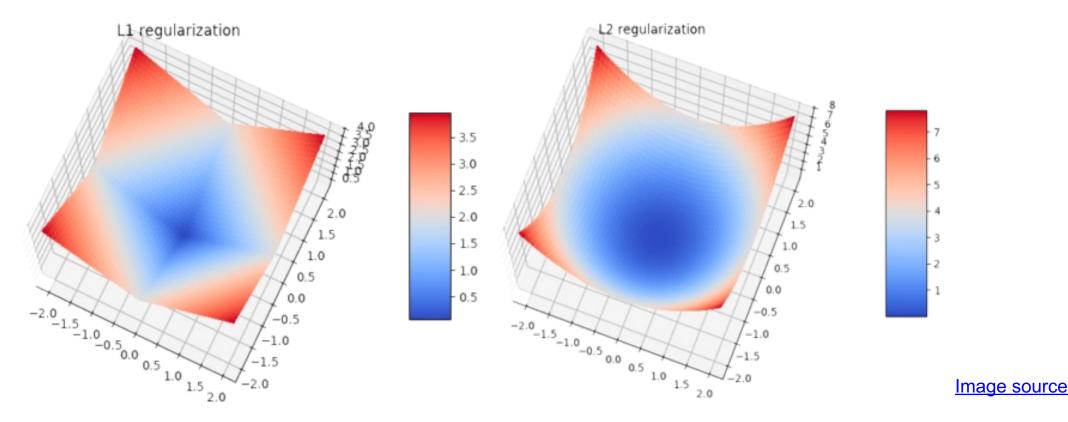
Y. Wu and K. He, Group Normalization, ECCV 2018

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  - Batch normalization
- Regularization

# Regularization

- Techniques for controlling the capacity of a neural network to prevent overfitting – short of explicit reduction of the number of parameters
- Recall: classic regularization: L1, L2



# Weight decay

• Generic optimization step:  $L(w) = L_{data}(w) + L_{reg}(w)$   $g_t = \nabla L(w_t)$   $s_t = optimizer(g_t)$   $w_{t+1} = w_t - \eta s_t$ 

- SGD with L2 regularization:  $L(w) = L_{data}(w) + \frac{\lambda}{2} ||w||^{2}$   $g_{t} = \nabla L_{data}(w_{t}) + \lambda w$   $w_{t+1} = w_{t} - \eta g_{t}$   $= (1 - \eta \lambda) w_{t} - \eta \nabla L_{data}(w_{t})$
- Optimization with weight decay:  $L(w) = L_{data}(w)$   $g_t = \nabla L(w_t)$   $s_t = \text{optimizer}(g_t)$   $w_{t+1} = (1 - \eta\lambda)w_t - \eta s_t$

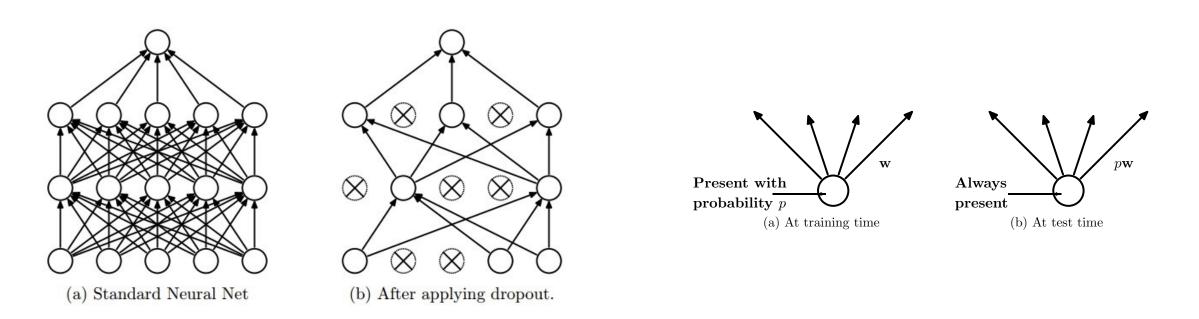
I. Loshchilov and F. Hutter, Decoupled Weight Decay Regularization, ICLR 2019 Adapted from J. Johnson

## Other types of regularization

- Adding noise to the inputs
  - Recall motivation of max margin criterion
  - In simple scenario (linear model, quadratic loss, Gaussian noise), this is equivalent to weight decay
  - Data augmentation is a more general form of this
- Adding noise to the weights
- Label smoothing
  - When using softmax loss, replace hard 1 and 0 prediction targets with "soft" targets of  $1 \epsilon$  and  $\frac{\epsilon}{c-1}$

# Dropout

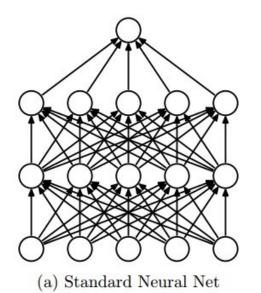
- At training time, in each forward pass, turn off some neurons with probability  $\boldsymbol{p}$
- At test time, to have deterministic behavior, multiply output of neuron by  $\boldsymbol{p}$

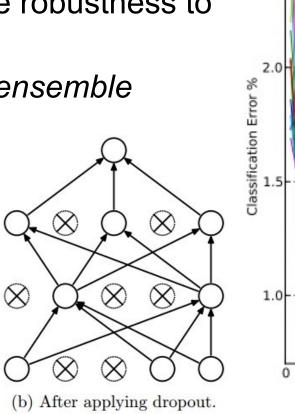


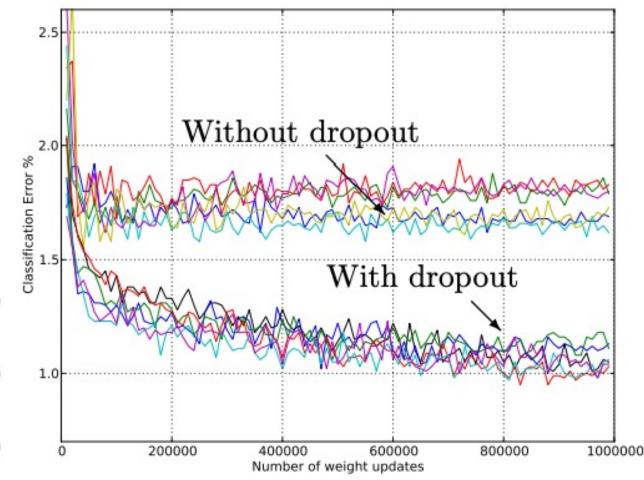
N. Srivastava, G. Hinton, A. Krizhevsky, I. Sutskever, R. Salakhutdinov. <u>Dropout: A Simple Way to Prevent Neural Networks from Overfitting</u>. JMLR 2014

# Dropout

- Intuitions
  - Prevent "co-adaptation" of units, increase robustness to noise
  - Train implicit ensemble







N. Srivastava, G. Hinton, A. Krizhevsky, I. Sutskever, R. Salakhutdinov. <u>Dropout: A Simple Way to Prevent Neural Networks from Overfitting</u>. JMLR 2014

## Current status of dropout

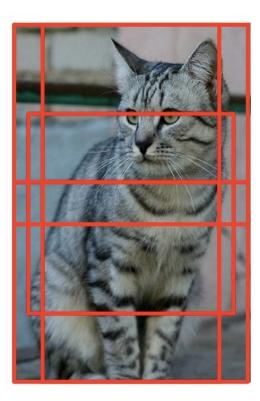
- Against
  - Slows down convergence
  - Made redundant by batch normalization or possibly even <u>clashes</u> with it
  - Unnecessary for larger datasets or with sufficient data augmentation
- In favor
  - Can still help for certain models and in certain situations: e.g., used in Wide Residual Networks

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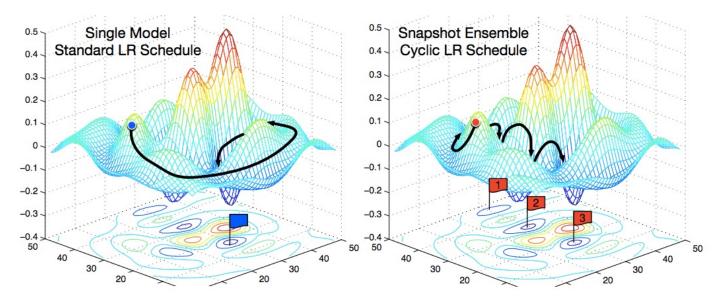
## Test time

- Average predictions across multiple crops of test image
  - There is a more elegant way to do this with *fully convolutional networks* (FCNs)



## Test time

- Ensembles: train multiple independent models, then average their predicted label distributions
  - Gives 1-2% improvement in most cases
  - Can take multiple snapshots of models obtained during training, especially if you *cycle* the learning rate (increase to jump out of local minima)



G. Huang et al., Snapshot ensembles: Train 1, get M for free, ICLR 2017

## **Important Considerations**

- 1. Data
- 2. Supervision
- 3. Loss functions
- 4. Optimization / Initialization
- 5. Inductive Bias

## **Development Process**

- 1. Collect lots of labeled data
- 2. Setup network architecture
- 3. Setup loss function
- 4. Sanity checks
  - 1. Is your data correct?
  - 2. Can you overfit to a small set?

#### 5. Hyperparameters

- 1. Learning hyperparameters: batch size, learning rates, how much to train, regularization, optimizer.
- 2. Architectural hyper-parameters: Non-linearities, #layers, #neurons, loss functions.

#### 6. Hacking

- 1. Reducing iteration time
- 2. Maximizing GPU utilization

#### Some take-aways

- Training neural networks is still a black art
- Process requires close "babysitting"
- For many techniques, the reasons why, when, and whether they work are in active dispute – read everything but don't trust anything
- It all comes down to (principled) trial and error
- Further reading: A. Karpathy, <u>A recipe for training neural networks</u>